

Programming in matlab

Introduccion to Synthetic Biology

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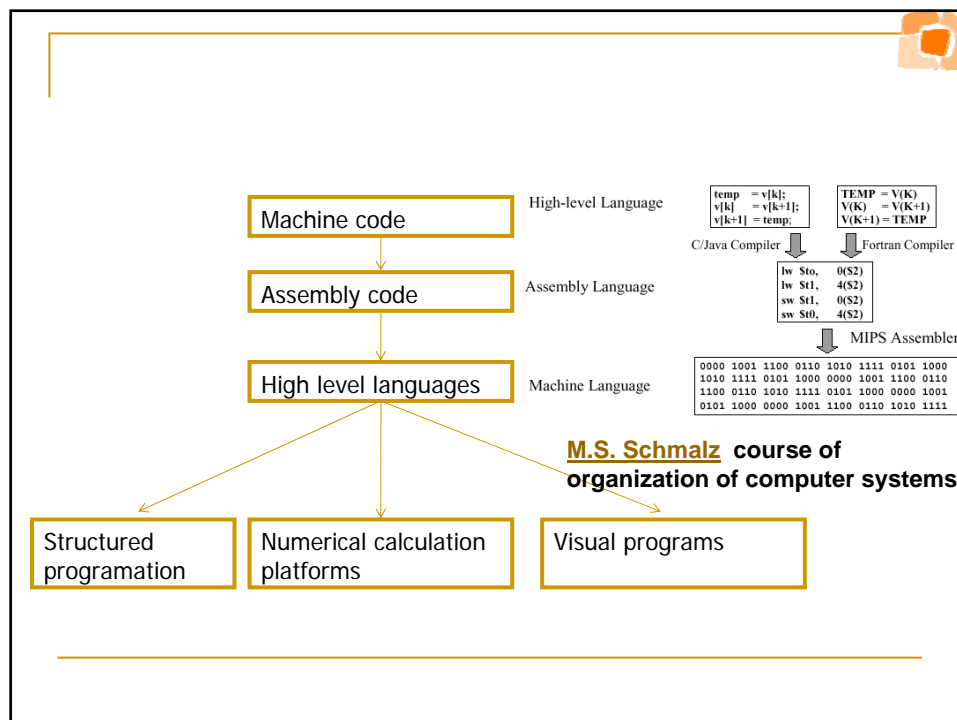


Overview

- Introduction to programming languages
- Basic matlab operations
- Programming in matlab
- Solving ODE with matlab

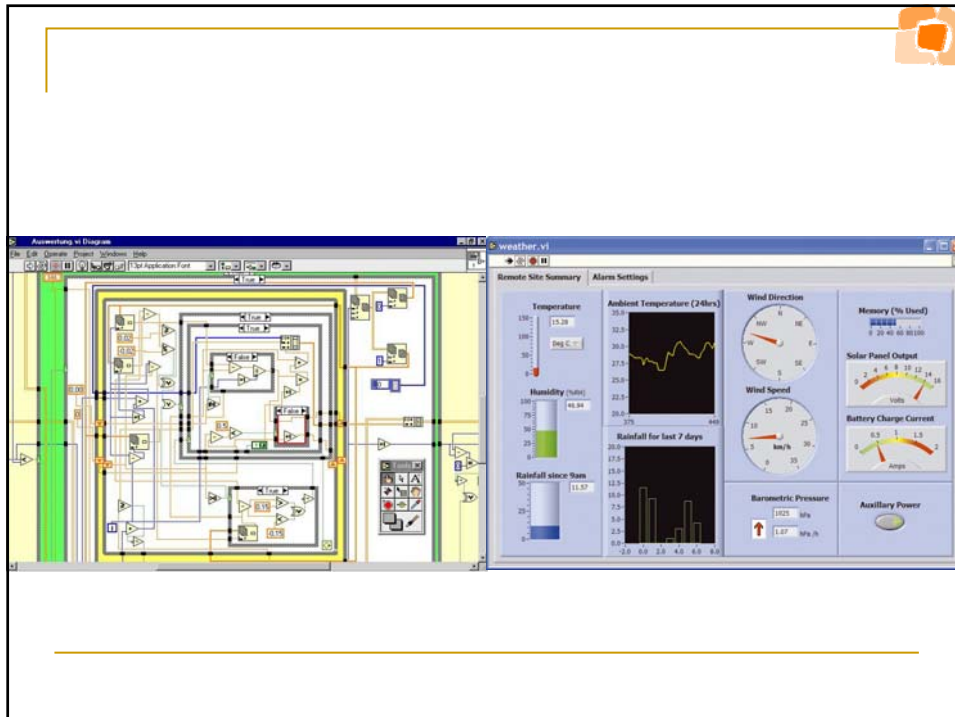
Programming languages

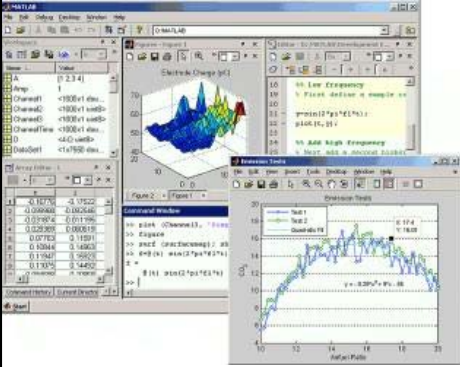
- They are designed to allow communication with devices, allowing them to perform different operations.
- First programming languages were predate to the first computers. They were punch cards according the desired function.
- After the invention of computers and the use of them to perform mathematical analysis, a lot of development has been obtained to make easier the programming for the user



High level programming

```
1      PROGRAM PRINCIPAL
2      PARAMETER (TAMMAX=99)
3      REAL A(TAMMAX)
4      10  READ (5,100,END=999) K
5      100 FORMAT(I5)
6      IF (K.LE.0.OR K.GT.TAMMAX) STOP
7      READ *,(A(I),I=1,K)
8      PRINT *,(A(I),I=1,K)
9      PRINT *, 'SUMA=', SUM(A,K)
10     GO TO 10
11  -99  PRINT *, ' "Todo listo" '
12     STOP
13     END
14  SUBPROGRAMA DE SUMATORIA EN C
15  FUNCTION SUM(V,N)
16     REAL :: V(N) ! Declaración de estilo nuevo
17     SUM = 0.0
18     DO 20 I = 1,N
19        SUM = SUM + V(I)
20  20    CONTINUE
21     RETURN
22     END
```





TaylorLab

El polinomio de Taylor $P_n(x)$, de grado n , tiene la característica de que sus primeras n derivadas coinciden con $f(x)$ en a , es decir:

$$P_n(a) = f(a), \quad P_n'(a) = f'(a), \quad \dots, \quad P_n^{(n)}(a) = f^{(n)}(a).$$

TS [x] = Taylor[f(x), {x, a, 5}]

$$f[a] + (-a+x) f'[a] + \frac{1}{2} (-a+x)^2 f''[a] + \frac{1}{6} (-a+x)^3 f^{(3)}[a] + \frac{1}{24} (-a+x)^4 f^{(4)}[a] + \frac{1}{120} (-a+x)^5 f^{(5)}[a]$$

D[TS[x], x]

$$f'[a] + (-a+x) f''[a] + \frac{1}{2} (-a+x)^2 f^{(3)}[a] + \frac{1}{6} (-a+x)^3 f^{(4)}[a] + \frac{1}{24} (-a+x)^4 f^{(5)}[a]$$

% f. (x=a)

$$f[a]$$

Table[D[TS[x], {x, n}] /. {x=a}, {n, 1, 5}]

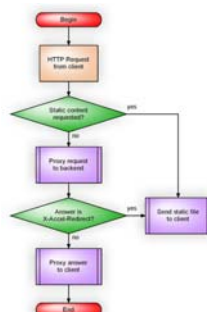
$$\{f[a], f'[a], f^{(2)}[a], f^{(3)}[a], f^{(4)}[a], f^{(5)}[a]\}$$

En las anteriores órdenes observe que :

$$D[TS[x], {x, n}] = TS^{(n)}(x) \quad \text{y}$$

$$D[TS[x], {x, n}] /. {x=a} = TS^{(n)}(a).$$

- Algorithm: Previous clear scheme of flow and operations in order to develop a task



```

graph TD
    Start([Start]) --> Request[HTTP Request from client]
    Request --> Check{Static content requested?}
    Check -- yes --> SendStatic[Send static file to client]
    Check -- no --> ProxyReq[Proxy request to backend]
    ProxyReq --> CheckBackend{Answer to ProxyRequest?}
    CheckBackend -- yes --> SendStatic
    CheckBackend -- no --> ProxyAnswer[Proxy answer to client]
    ProxyAnswer --> End([End])
  
```

Matlab

- ❑ Introduction.
 - ❑ Help
 - ❑ Matrix operations
 - ❑ Matrix functions.
 - ❑ Graphyics.
 - ❑ Programming.
 - ❑ Numerical analysis
-

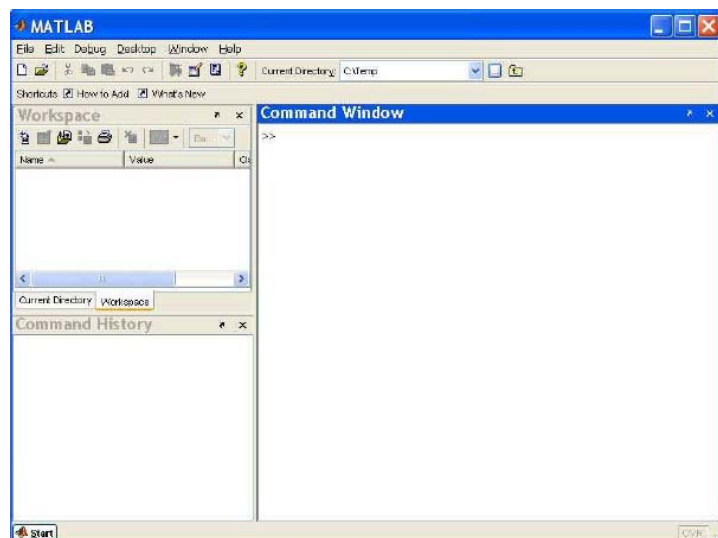
■ ¿What is Matlab?, MATrix LABoratory

- ❑ MATLAB is a program for performing numerical calculations with matrix and vectors.
 - ❑ As a particular case it can perform operations with escalars (reals and complex).
 - ❑ It can also perform graphical representations of the results and nowadays have many useful applications.
-

Matlab have several packages not included in the standard version which extend its capabilities:

- Optimization toolbox
- Statistical toolbox
- Simbiology
- Symbolic math toolbox
- And the like...

http://www.mathworks.com/products/product_listing/index.html





The basic Matlab elements are: constants, variables, operations, expressions and functions.

Numerical constants:

- Integers: 2 35 -48
- Reals: 2. -35.2 48.45
 - 16 significant figures
 - [2.2250e-308 1.7e+308].
- Complex numbers: $2+3i$ $4*j$ $i,j=(-1)^{1/2}$

Elementary operators:

addition: + product: * Exponential: ^
Subtraction: - Division: /



Variable: it is the brand which identifies a part of the memory.

Matlab makes differences between capitals and no capital letters

To define a variable:

```
>>a=3.2 ; b=53.65
```

To see the defined variables:

```
>> who
```

To remove a variable

```
>> clear variable1 variable2
```

If a variable is between " " it is a text variable

```
>>c='matlab is nice'
```

Numerical expressions: A set of functions and variables already related by arithmetic operators.



Format: by default matlab uses short format but

- >> format long (14 cifras significativas)
- >> format short (5 cifras significativas)
- >> format short e (notación exponencial)
- >> format long e (notación exponencial)
- >> format rat (aproximación racional)

Predefined variables:

$i = (-1)^{1/2}$ $\pi = \pi$ $\text{Inf} = \infty$ $\text{NaN} = \text{Undefined solution}$
 $\text{date} = \text{date}$
 $\text{rand} = \text{Random numbers between 0 and 1}$

Functions:

name(argument)

- sqrt(x) square root
- abs(x) module of x
- conj(z) conjugated number
- real(z), imag(z)
- exp(x)
- sin(x) asin(x) $[-\pi/2 \ \pi/2]$ cos(x) acos(x) $[0 \ \pi]$ tan(x)
atan(x) $[-\pi/2 \ \pi/2]$ angle(z) log(x), log10(x)
- rats(x), rem(x,y), round(x), sign(x)

Help comands:

- help
- what files .m and .mat of the directory
- dir files of the present directory

Basic comandands

- type File_name Show the file content
- delete File_name
- cd
- pwd show the directory
- clr clean the memory of the variables
- which File_name
- startup.m boot file.

Saving in a file the commands of a sesion

```
>> diary File_name
```

```
...
```

```
>> diary off
```

VECTORS Y MATRIX

- Basis of matlab (Matrix Laboratory).

```
» A=[1 3 5; 6 9 2; 4 8 7]
```

```
A =
```

1	3	5
6	9	2
4	8	7

```
» det(A)
```


```
ans =
```

```
5
```

```
» A^2+3*A
```

```
ans =
```

42	79	61
86	142	68
92	164	106



File vectors: The elements are separated by spacebars or comma

```
>> v = [2 3 4]
```

Vectores columna: The elements are separated by intro or by ";"

```
>> w = [2;3;4;7;9;8]
```

```
>> length( vector name) Dimension of the vector.
```

Generating vectors:

- Specifying the increment of its components $v=a:h:b$;
 - specifying its dimension `linspace(a,b,n)`; The increment is given by $k=(b-a)/(n-1)$
 - Components separated using a logarithmic `logspace(a,b,n)` 10^a and 10^b .
 - By hand $v(3)=4$
-



Operating with scalars:

$v+k$

$v-k$

$v*k$

v/k

$k./v$

$v.^k$

$k.^v$

Operating with vectors:

$v+w$

$v-w$

$v.*w$

$v./w$

$v.^w$

scalar product of vectors

$v*w$

Some specific functions:

`sum(v)`

`prod(v)`

`v'` (files \leftrightarrow columns)

`dot(v,w)` scalar product

`cross(v,w)` vectorial product

`max(v)`

Matrix

To define a matrix it is not necessary to define its size

Example of matrix definition:

» **A=[1 2 3; 4 5 6; 7 8 9]**

The response is

A =

1 2 3

4 5 6

7 8 9

» Inv()

» A'

To have access to the vector elements we write x(3);

To have access to the elements of a matrix A(1,2) or A(4)

Matrix operators:

+

-

*

.

^

\

/

.* product element by element

./ y \. división element by element

.^ power element by element



Functions with matrix:

- `diag(A)`
- `sum(diag(A))`
- `diag(A,k)`
- `norm(A)`
- `det(A)`
- `full(A)`
- `find(a)`
- `inv(A)`
- `rank(A)`
- `eig(A), [v,D]=eig(A)`

Generating matrix:

- `zeros(n,m)`
- `ones(n,m)`
- `eye(n,m)`
- `rand(n,m)`
- `diag(v), diag(v,k)`
- `sparse(i,j,c,m,n)`

POLYNOMIALS



The polynomials are represented by a file vector of dimension $n+1$ being n the degree of the polynomia

Having the polynomia

$$x^3 + 2x$$

it is represented by

```
>> pol1=[1 0 2 0]
```

```
>> root=roots(pol1) (give the root)
```

A polynomia can be rebuilt

```
>> p=poly(raices)
```

Example 1:

```
pol2=[2 4 0 1]; % Definition of the polynomia  $2x^3+4x^2+1$ 
```

```
raices=roots(pol2) % root calculation
```

```
pol2_n=poly(raices) % rebuilt polynomia
```

Example 2:

```
A=[1 2 3 ; 2 3 4; 4 2 5]; p=poly(A) % Char pol
```

```
roots(p) % eigenvalues of A
```

To calculate the value of a polynomia:

```
>>y=polyval(p,x)
```

To multiply or divide two polynomia:

```
>>conv(p1,p2)
```

```
>>deconv(p1,p2)
```

```
>>[p4,r] = deconv(p3,p2)
```

```
>>[r,p,k] =residue(p1,p2)
```

$$\frac{p1(x)}{p2(x)} = \frac{r(1)}{x - p(1)} + \dots + \frac{r(n)}{x - p(n)} + k(x)$$

```
>>polyder(p)
```

Linear Equations

$$Ax=b$$

Compatibility of a system:

```
>>rank(A)-rank([A,b])
```

Example:

```
x=ones(4,4);v=[2 2 2 2];y=x+diag(v)
```

```
rank(y)
```

3	1	1	1
1	3	1	1
1	1	3	1
1	1	1	3

$$Ax=b$$

If we have a square matrix:

```
>>Ainv=inv(A)
```

```
>>x=Ainv*b
```

Or

```
>>x=A\b
```

GRAPHYCS

These functions represent a set of data:

- `plot(a,b,M)`
- `loglog(a,b,M)`
- `semilogx(a,b,M)`
- `semilogy(a,b,M)`

To plot functions introduced as key-character chain :

- `Fplot(f,[a b],M)`

To represent symbolic expressions in a plane:

- `Ezplot(f,[a b])`
-

Numerical Analysis

To develop the numerical analysis of functions, matlab has predefined several functions and packages that can be used in an easy way.


Local minimum of a function

`min=fminbnd('function',a,b,opciones)`

Example:

Calculus of the local $f(x)=3x^4-4x^3$ in $[-1 \ 2]$

`fminbnd('3*x^4-4*x^3',-1,2)`



```
fminbnd('-(3*x^4-4*x^3)',-1,2)
```

```
fminbnd('-(3*x^4-4*x^3)',0,2)
```

Calculating the minimum of a several variable function

```
min=fminsearch('funcion',x0)
```

Here we give a point in which we want to minimize the function

Example

Minimize the function $f(x)=\sin(xy)$ around $[0,0]$

```
fminsearch('sin(x(1)*x(2))',[0,0])
```



To calculate the zeros of a function

```
root=fzero('funcion',x0)
```

We should give the initial point x_0 to begin iterations

example:

$\sin(x)-2\cos(2x)+x^2=\pi^2-2$.

suppose that the function changes its sign at this interval $[0,10]$

```
x=0;eval('sin(x)-2*cos(2*x)+x^2-pi^2+2')
```

```
x=10;eval('sin(x)-2*cos(2*x)+x^2-pi^2+2')
```

```
x0=5
```

```
x=fzero('sin(x)-2*cos(2*x)+x^2-pi^2+2',5)
```

```
eval('sin(x)-2*cos(2*x)+x^2-pi^2+2')
```

Intregation:

.-Integration of unidimensional functions

quad

quadl

.-Double integration

dblquad

Example

```
ia=quad('sin(x)+1',0,2*pi); %(6.2832)
```

```
xmin=pi;xmax=2*pi;
```

```
ymin=0;ymax=pi;
```

```
result=dblquad('y*sin(x)+x*cos(y)',xmin,xmax,ymin,ymax)
```

```
%-9.8698
```

```
ia=quad('sin(x).^2.*cos(x).^2',0,4*pi) %1.0051e-030
```

```
ial=quadl('sin(x).^2.*cos(x).^2',0,4*pi) %1.5708
```

Solving differential equations

Solving problems of initial values for differential equations.


$$[T,Y]=\text{solver}('F',tspan,y0)$$

.- solver Algorithm used to solve the differential equation: ode45, ode23, ode113, ode15s,ode23s.

.-F string contains the name of the file with the differential equation.

.-tspan time integration vector [t0 tfinal]

.-y0 column vector of the initial conditions.



function	type	method
ode45	Non-stiff dif ec	Medium order
ode23	Non-stiff dif ec	Low order
ode113	Non-stiff dif ec	Variable order
ode15s	stiff dif ec	Variable order
ode23s	stiff dif ec	Low order



Example

$$y_1'' - \mu(1 - y_1^2)y_1' + y_1 = 0$$
$$\mu > 0$$

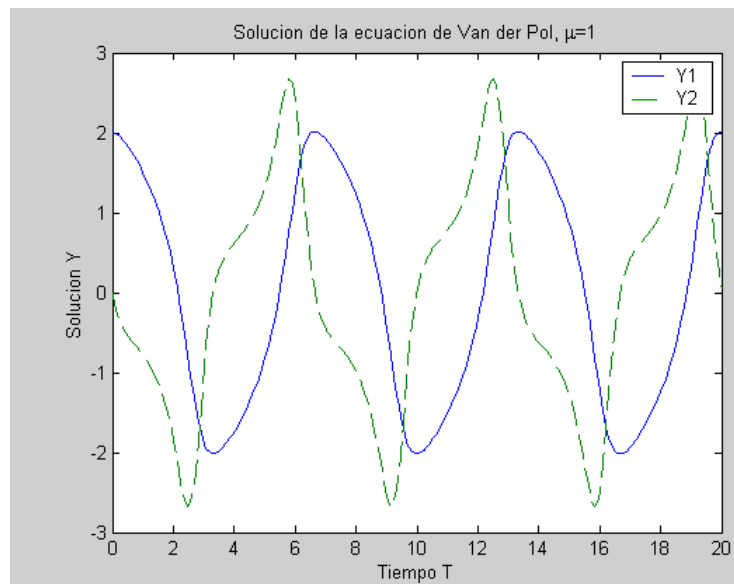
Rewriting the system:

$$y_1'' = y_2$$
$$y_2' = \mu(1 - y_1^2)y_2 - y_1$$

```

function dy=vdp1(t,y)
dy=[y(2); (1-y(1)^2)*y(2)-y(1)];
Call solver
[T,Y]=ode45('vdp1',[0 20],[2;0]);
plot(T,Y(:,1),'-',T,Y(:,2),'--')
title('Solucion de la ecuacion de Van der Pol, \mu=1')
xlabel('Tiempo T')
ylabel('Solucion Y')
legend('Y1','Y2')

```



Solving ODE analitically

```
R=Dsolve('eq1,eq2,...', 'cond1,cond2,...','v')
```


- Symbolically it solves ODE(s) specified by eq1, eq2,... using v as the independent variable and the boundary and/or initial condition(s) specified by cond1,cond2,....
- If dsolve cannot find an explicit solution, it attempts to find an implicit solution. When dsolve returns an implicit solution, it issues a warning. If dsolve cannot find either an explicit or an implicit solution, returns the empty sym. A numeric solution with ode23 or ode45 functions.

Examples

```
>>dsolve('Dx = -a*x')  
C1*exp(-a*t)
```

```
>>dsolve('Dy = a*y', 'y(0) = b')  
b*exp(a*t)
```

```
>> r=dsolve('Dx = y', 'Dy = -x','x(0)=0','y(0)=1','t')  
r =  
    x: [1x1 sym]  
    y: [1x1 sym]  
>> a=r.x  
a =sin(t)
```



ezplot(function, [a b]) Easy to be used for plotting

```
sol = dsolve('Dy=t*y^2','y(-2)=y0','t')
for y0=-0.4:0.2:2
    ezplot( subs(sol,'y0',y0) , [-2 2])
    hold on
end
hold off
axis tight
```



PROGRAMMING

All the comand files in matlab have the extension .m:

- Function files: The first line is executable and begin with the word function
 - Program files: Comand sequence.
-



Input output (IO) comandos

- **input**: introduces data from keyboard
variable=input('mensaje a pantalla');
 - **disp**: shows text
disp('El algoritmo no ha convergido')
 - **menu**: creates an option menu
option=menu('title','option1',... 'optionp')
 - **error**('condition','message'): gives information about a problem in the program execution
-



Programing functions

First line represents the execution line

function arg_salida=nombre_funcion(arg_entrada)

Then we can add all the commands that we want according to the purpose of the function

Return: gives back the control to the main program

Definition of a function which calculates de temperature knowing the pressure and the volume for an ideal gas

```
function t=gases(p,v,n)
%t=gases(p,v,n)
%funcion que considera la ley de los gases ideales
%Argumentos de entrada:
%presion p (atmosferas)
%volumen v (litros)
%número de moles n
%Argumentos de salida:
%temperatura t (grados kelvin)
%R=0.0821 atm.litro/mol.grado
R=0.0821
t=p*v/(n*R);
```

Saved as gases.m

```
temp=gases(20,10,10)
```

- The m-file can be executed only after >> or in another file
- The m-file does not use input arguments
- The variables of a function are locals and the variables of a file are global.

global variable

echo writes each comand of the file in the screen

pause stops the execution of a program, unless the user push a key.

keyboard same utility although it allows to introduce commands during the execution of the program.



Bucles. Nested Bucles

```
for k=n1:incre:n2  
end
```

```
for k=vector_columna  
end
```

Break: breaks the execution sequence



Condicional control structures

if	if	if	if	
end	else	elseif	elseif	while
	end	end	else	end
			end	

Logical and order operators

- <, <=, >, >=

- ==, ~=

- OR: | AND: & NOT: ~

The result of this operations will be 1 or 0

Other functions:

xor(x,y): "or" 0 if x or y are different from 0

any(x): True if any element of a vector is a nonzero number or is logical 1 (TRUE)..

all(x): True if all elements of a vector are nonzero.

isempty(x): 1 if the matrix x is empty.

isequal(x1,x2,...,xn): 1 if all the matrix are identical.

```
switch expresion
case expresion_0
    comandos_0 que deben ejecutarse
case expresion_1
    comandos_1 que deben ejecutarse
case expresion_2
    comandos_2 que deben ejecutarse
otherwise
    comandos escoba que deben ejecutarse
end
```

IO to external files

`fread` and `fscanf` to read

`fprintf` and `fwrite` to write

The general procedure is:

- Open the file that you want to read or write.
- Put the write or read pointer on the desired position.
- Read or write variables.
- Close the file.

-Open the file `fopen`

`ident=fopen('nombre de fichero',type of file)`

`ident` saves the identification number, if it is -1 the file can not be opened

-Close the file `fclose`

`fclose(ident)`

`fclose('all')`

`verif=fclose('all')`

-Putting the pointer.

1.-Put the pointer in the beginning of the file:

`frewind(ident)`

2.-Put the pointer inside a file

`test=fseek(ident,posi,'origen')`



This sentence put the pointer of the file ident in the position indicated by posi:

- .-If $posi > 0$ move posi bytes upwards.
- .-If $posi < 0$ move posi bytes downwards.
- .-If $posi = 0$ no movement.

The variable origen shows from which position the pointer begins to move:

- .-'bof': Beginning of the file.
- .-'cof': Position that it have now.
- .-'eof': End of the file.

fseek turns back the test variable (-1 if something go wrong).

To know the pointer position: $posi = ftell(ident)$



Reading formatted data:

$[data, counter] = fscanf(ident, 'format', how_many)$

- 1.-Read data from the file ident.
- 2.-The data are saved in data.
- 3.-how_many shows how many data are going to be read.
 - .-k
 - .-[n,m] : The data are stored column to column
 - .-inf : all the data of the file.
- 4.-counter shows how many data have been read
- 5.-format: format to read.

%d: decimals	%g: neither considered nor significant 0
%e: Exponential notation	%s: character variable
%f: fix point notation	

Reading not formatted data

```
data=fread(ident,how_many,'precision')
```

Writing in a file

Formatted data:

```
counter=fopen(ident,'format',data,controls)
```

\n new line


\t goes forward to the next tab position

Not formatted data:

```
counter=fopen(ident,data,'precision')
```

Example:

```
function root2=sole2(a,b,c)
%root2=sole2(a,b,c)
%solve an equation of second order
%ax^2+bx+c=0, a~0
%
if (nargin ~=3)
    error('the number of arguments must be 3')
end
discr=b^2-4*a*c;
root2=[];
if(discr==0)
    root2=-b/(2*a);
    disp(['Double root2=',num2str(root2)])
    return
elseif(discr>0)
```



```

root2(1)=(-b+sqrt(discr))/(2*a);
root2(2)=(-b-sqrt(discr))/(2*a);
disp(['Simple Real Roots=',num2str(root2)])
return
else
root2(1)=(-b+sqrt(-discr)*i)/(2*a);
root2(2)=(-b-sqrt(-discr)*i)/(2*a);
disp(['Imaginary Roots=',num2str(root2)])
return
end

```

This function is executed:


```

root2=sole2(2,3,1);
root2=sole2(1,0,1);

```

Example 3:

Develop a program to multiply complex matrix without using the predefined matlab functions:



```

A=[1 2;3 4];
B=[2 3;4 5];
C=[3 4;5 6];
D=[4 5;6 7];
E=zeros(2,2);F=zeros(2,2);
for i=1:1:2;
    for j=1:1:2;
        E(i,j)=A(i,j)*C(i,j)-B(i,j)*D(i,j)
        F(i,j)=A(i,j)*D(i,j)+B(i,j)*C(i,j)
    end
end
fid = fopen('exp.txt','wt');

for i=1:1:2;
    for j=1:1:2;
        if (F(i,j)>0)
            fprintf(fid,'%i + %i \n',E(i,j),F(i,j));

        else
            fprintf(fid,'%i %i \n',E(i,j),F(i,j));
        end
    end
    fprintf(fid,'\n');
end

fclose(fid)

```


Example 3:

Reading data

Name	Analysis	Algebra	Physics	Statistics
Fernando Gómez Pereira	3	6	5	7
Susana Rodríguez Pérez	7	4	3	1
Carlos Leis Álvarez	8	9	7	9
Arturo Gómez Álvarez	5	4	5	9
Silvia Tais Álvarez	10	9	10	9
Andrea Gallego Nimes	3	3	2	4
Alicia Caballero Leis	6	8	8	5
Antonio Fraga Gómez	5	7	6	5
Beatriz Machado Gómez	4	3	5	4
Laura Tobío Manzanal	7	8	5	9
Juan Rico Fraga	4	7	5	5
Andrés Pena Gómez	6	8	5	6
Luis Blanco Villa	8	6	6	4
Sandra Puentes Gallego	9	9	7	9
Isolina Prieto Gómez	5	5	6	6
Teresa Sieiro Gon	4	2	5	3
Ricardo López Amigo	8	6	2	9

Example 2:

```
ident=fopen('datos.m');
frewind(ident)
variables=[];
for i=1:5
    variable=fscanf(ident,'%s',1);
    long_v(i)=length(variables)+length(variable);
    variables=[variables variable];
    if(i==1)
        fprintf(1,'\t%s\t\t',variable)
    else
        fprintf(1,'\t%s\t',variable)
    end
end
nombres=[];
califica=[];
```



```
for i=1:17
    nombre=fscanf(ident,'%s,%c',1);
    apellido1=fscanf(ident,'%s,%c',1);
    apellido2=fscanf(ident,'%s,%c',1);
    l=3*(i-1)
    long_n(l+1)=length(nombres)+length(nombre);
    long_n(l+2)=long_n(l+1)+length(apellido1);
    long_n(l+3)=long_n(l+2)+length(apellido2);
    nombres=[nombres nombre apellido1 apellido2];
    califica=[califica; fscanf(ident,'%i',4)];
    fprintf(1,'\n%9s %s %9s',nombre, apellido1, apellido2)
    fprintf(1,'\t%i\t\t%i\t\t%i\t\t%i',califica(i,:))
end
fclose(ident)
```



Bibliography

- Matlab manual.
<http://www.mathworks.com/access/helpdesk/help/techdoc/matlab.shtml>